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Here you find documentation for all of Sage’s features, illustrated with lots of examples. A thematic index follows. This documentation is licensed under the Creative Commons Attribution-Share Alike 3.0 License.
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